

$$VP = \chi_{H_2O} \times VP_{H_2O} \quad \Delta T = -k_f m$$

Solutions – Colligative Properties/Practice

Name: Key

1. What is the vapor pressure of water above a 0.20 m glucose (C₆H₁₂O₆) solution at 20°C? Use vapor pressure data from your text book. (VP H₂O at 20°C = 17.5 mmHg) (ans: 17.4 mmHg)

0.20 m glucose - 1000g H₂O x 1 mol / 18g = 55.49 mol.
 1 kg H₂O

$$\chi_{H_2O} = \frac{55.4}{55.4 + 0.02} = 0.9964 \quad \left\| \begin{aligned} VP_f &= 0.9964 \times 17.55 \text{ mmHg} \\ &= \boxed{17.44 \text{ mmHg}} \end{aligned} \right.$$

2. Determine the freezing point of a

- a) 0.25 m urea in water (ans: -0.47°C) $k_f = -1.88^\circ\text{C}/m$

$$\Delta T = -k_f m = -(1.86^\circ\text{C}/m \times 0.25 m) = -0.465^\circ\text{C}$$

$$\Delta T = -0.465^\circ\text{C} = T_f - T_i$$

$$-0.465^\circ\text{C} = T_f - 0.00$$

$$\boxed{T_f = -0.47^\circ\text{C}}$$

- b) 5.0% para dichlorobenzene, C₆H₄Cl₂ (MW = g/mol) by mass in benzene (C₆H₆). (ans: 3.70°C) $k_f = -5.12^\circ\text{C}/m$

$$\textcircled{1} \frac{5.0g \text{ C}_6\text{H}_4\text{Cl}_2}{95 \times 10^{-3} \text{ kg C}_6\text{H}_6} \times \frac{1 \text{ mol}}{147g \text{ C}_6\text{H}_4\text{Cl}_2} = \boxed{0.358 m}$$

$$\textcircled{2} \Delta T = -5.12^\circ\text{C}/m \times 0.358 m = -1.83^\circ\text{C}$$

$$\textcircled{3} \Delta T = -1.83^\circ\text{C} = T_f - T_i = T_f - 5.53^\circ\text{C} \quad \boxed{T_f = 3.70^\circ\text{C}}$$

3. Determine the boiling points of

- a) 0.44 m naphthalene in benzene (ans: 81.2°C) $k_b = 2.53^\circ\text{C}/m$

$$\Delta T = 2.53^\circ\text{C}/m \times 0.44 m = 1.11^\circ\text{C}$$

$$\Delta T = 1.11^\circ\text{C} = T_f - T_i = T_f - 80.1^\circ\text{C}$$

$$\boxed{T_f = 81.2^\circ\text{C}}$$

- b) 1.8 M sucrose (C₁₂H₂₂O₁₁) in water (d= 1.23 g/mL) (ans: 101.5°C)

$$\frac{1.8 \text{ mol}}{1 \text{ L soln}} \left[\begin{aligned} &1000 \text{ mL soln} \times \frac{1.23 \text{ g soln}}{1 \text{ mL}} = 1230 \text{ g soln} \\ &1.8 \text{ mol} \times 342.3 \text{ g/mol} = 616 \text{ g sucrose} \\ &1230 \text{ g} - 616 \text{ g} = \boxed{610 \text{ g H}_2\text{O}} \end{aligned} \right.$$

$$\textcircled{2} \left[\frac{1.8 \text{ mol}}{0.610 \text{ kg}} = 2.9 m \right.$$

$$\Delta T = 0.512^\circ\text{C}/m \times 2.9 m = 1.5^\circ\text{C}$$

$$\Delta T = 1.5^\circ\text{C} = T_f - T_i = T_f - 100$$

$$\boxed{T_f = 101.5^\circ\text{C}}$$

4. How many grams of naphthalene, $C_{10}H_8$, would you add to 50.0 g benzene (C_6H_6 , $F_{pt.} = 5.53^\circ C$), to produce a solution that has the same freezing point as pure water? (ans: 6.92 g)

$$T_f = 0.00^\circ C \quad T_i = 5.53^\circ C \quad \leftarrow 0^\circ C$$

$$\Delta T = T_f - T_i = 0 - 5.53 = -5.53^\circ C$$

$$-5.53^\circ C = -k_f m = -5.12^\circ C/m \times m$$

$$m = \frac{-5.53^\circ C}{-5.12} = \frac{1.08 \text{ mol naph}}{1 \text{ kg benzene}}$$

$$\frac{1.08 \text{ mol naph}}{1000 \text{ g benz.}} \times 50 \text{ g benz} \times \frac{128.2 \text{ g naph}}{1 \text{ mol naph}} = \boxed{6.92 \text{ g}}$$

5. A 1.45 g sample of an unknown compound is dissolved in 25.00 mL benzene (C_6H_6 , $d=0.879 \text{ g/mL}$). The solution freezes at $4.25^\circ C$. What is the molar mass of the unknown? (ans: 264 g/mol)

$$\Delta T = (4.25 - 5.53)^\circ C = -1.28^\circ C$$

$$\Delta T_f = -k_f m \quad m = \frac{\Delta T}{-k_f} = \frac{-1.28^\circ C}{-5.12^\circ C/m} = 0.250 m$$

$$25.00 \text{ mL benz} \times 0.879 \frac{\text{g}}{\text{mL}} = 22.0 \text{ g benz} \equiv 0.022 \text{ kg benz.}$$

$$0.250 m = \frac{\text{mol}}{0.022 \text{ kg benz.}} \quad \text{mol} = 0.250 m \times 0.022 = 0.00550 \text{ mol}$$

$$\boxed{\frac{1.45 \text{ g}}{0.00550 \text{ mol}} = 264 \text{ g/mol}}$$

6. Predict the approximate freezing points of: 0.10 m glucose ($C_6H_{12}O_6$), 0.10 m $CaCl_2$, 0.10 m CH_3COOH and 0.10 m KI.

$$\Delta T = -k_f m = -1.86^\circ C/m \times 0.1 = -0.19^\circ C$$

0.10 m glucose $i = 1$ $T_f = \boxed{-0.19^\circ C}$

0.1 m $CaCl_2$ $i = 3$ $T_f = \boxed{-0.57^\circ C}$

0.1 m CH_3COOH $i = 1$
(same ionization)

$$\boxed{> -0.19^\circ C}$$

0.10 m KI $i = 2$

$$T_f = (-0.19 \times 2) = \boxed{-0.38^\circ C}$$